

Directions: Find the perimeter of the figure given the points on a coordinate plane.

1. A(2, 3), B(5, -3), C(2, -3)

$$AB: \sqrt{(5-2)^2 + (-3-3)^2} = \sqrt{3^2 + (-6)^2} = \sqrt{9+36} = \sqrt{45} = 3\sqrt{5}$$

$$BC: \sqrt{(2-5)^2 + (-3-(-3))^2} = \sqrt{(-3)^2 + 0^2} = \sqrt{9} = 3$$

$$AC: \sqrt{(2-2)^2 + (-3-3)^2} = \sqrt{0^2 + (-6)^2} = \sqrt{36} = 6$$

$$9 + 3\sqrt{5} \text{ units}$$

2. C(0, 3), A(-1, -1), K(4, 2), E(3, -2)

$$CA: \sqrt{(-1-0)^2 + (-1-3)^2} = \sqrt{(-1)^2 + (-4)^2} = \sqrt{1+16} = \sqrt{17}$$

$$AK: \sqrt{(4-(-1))^2 + (2-(-1))^2} = \sqrt{5^2 + 3^2} = \sqrt{25+9} = \sqrt{34}$$

$$KE: \sqrt{(3-4)^2 + (-2-2)^2} = \sqrt{1^2 + (-4)^2} = \sqrt{1+16} = \sqrt{17}$$

$$EC: \sqrt{(3-0)^2 + (-2-3)^2} = \sqrt{3^2 + (-5)^2} = \sqrt{9+25} = \sqrt{34}$$

$$2\sqrt{17} + 2\sqrt{34} \text{ units}$$

3. P(5, -1), L(1, 2), U(9, -4), M(4, 4)

$$PL: \sqrt{(1-5)^2 + (2-(-1))^2} = \sqrt{(-4)^2 + 3^2} = \sqrt{16+9} = \sqrt{25} = 5$$

$$LU: \sqrt{(9-1)^2 + (-4-2)^2} = \sqrt{8^2 + (-6)^2} = \sqrt{64+36} = \sqrt{100} = 10$$

$$UM: \sqrt{(4-9)^2 + (4-(-4))^2} = \sqrt{(-5)^2 + 8^2} = \sqrt{25+64} = \sqrt{89}$$

$$PM: \sqrt{(4-5)^2 + (4-(-1))^2} = \sqrt{(-1)^2 + 5^2} = \sqrt{1+25} = \sqrt{26}$$

$$15 + \sqrt{26} + \sqrt{89} \text{ units}$$

4. S(0, 3), M(-4, 3), I(2, 5), T(-8, 1), E(6, 2)

$$SM: \sqrt{(-4-0)^2 + (3-3)^2} = \sqrt{(-4)^2 + 0^2} = \sqrt{16} = 4$$

$$MI: \sqrt{(2-(-4))^2 + (5-3)^2} = \sqrt{6^2 + 2^2} = \sqrt{36+4} = \sqrt{40} = 2\sqrt{10}$$

$$IT: \sqrt{(-8-2)^2 + (1-5)^2} = \sqrt{(-10)^2 + (-4)^2} = \sqrt{100+16} = \sqrt{116} = 2\sqrt{29}$$

$$TE: \sqrt{(6-(-8))^2 + (2-1)^2} = \sqrt{14^2 + 1^2} = \sqrt{196+1} = \sqrt{197}$$

$$ES: \sqrt{(6-0)^2 + (2-3)^2} = \sqrt{6^2 + (-1)^2} = \sqrt{36+1} = \sqrt{37}$$

$$4 + 2\sqrt{10} + 2\sqrt{29} + \sqrt{197} + \sqrt{37} \text{ units}$$

Directions: Find the area of each polygon with the given coordinates.

5. $C(-2, 4), U(-2, 0), P(1, 3)$

$b: 4$
 $h: 3$

$A = \frac{1}{2}bh \Rightarrow \frac{1}{2}(4)(3) = 6u^2$

6. $K(4, 5), A(3, 4), T(6, 1), S(7, 2)$

$KA: \sqrt{(3-4)^2 + (4-5)^2} = \sqrt{(-1)^2 + (-1)^2} = \sqrt{1+1} = \sqrt{2}$

$AT: \sqrt{(6-3)^2 + (1-4)^2} = \sqrt{3^2 + (-3)^2} = \sqrt{9+9} = \sqrt{18}$

$\sqrt{18} = 3\sqrt{2}$

2×9
 3×3

$3\sqrt{2} \cdot \sqrt{2} =$

$3\sqrt{4} = 3 \cdot 2 = 6u^2$

7. $M(-1, -5), A(0, -2), T(3, -3), H(2, -6)$

$MA = \sqrt{(0-(-1))^2 + (-2-(-5))^2} = \sqrt{1^2 + 3^2} = \sqrt{4+9} = \sqrt{13}$

$\sqrt{13} \cdot \sqrt{10} = \sqrt{130}u^2$

$MH: \sqrt{(2-(-1))^2 + (-6-(-5))^2} = \sqrt{3^2 + (-1)^2} = \sqrt{9+1} = \sqrt{10}$

Directions: Find the coordinates that partitions the segment at the given ratio.

8. Partition the line segment \overline{WM} at a ratio of $\frac{a}{b} = \frac{2}{5}$, where $W(-4, 2)$ and $M(3, 9)$.

$(-4 + \frac{2}{7}(3-(-4)), 2 + \frac{2}{7}(9-2)) \rightarrow (-4 + \frac{2}{7}(7), 2 + \frac{2}{7}(7)) \rightarrow (-4+2, 2+2)$

$(-2, 4)$

9. Partition the directed line segment \overline{GM} at point Q, such that Q lies $\frac{2}{5}$ of the way, given $G(-2, -3)$ and $M(1, 7)$.

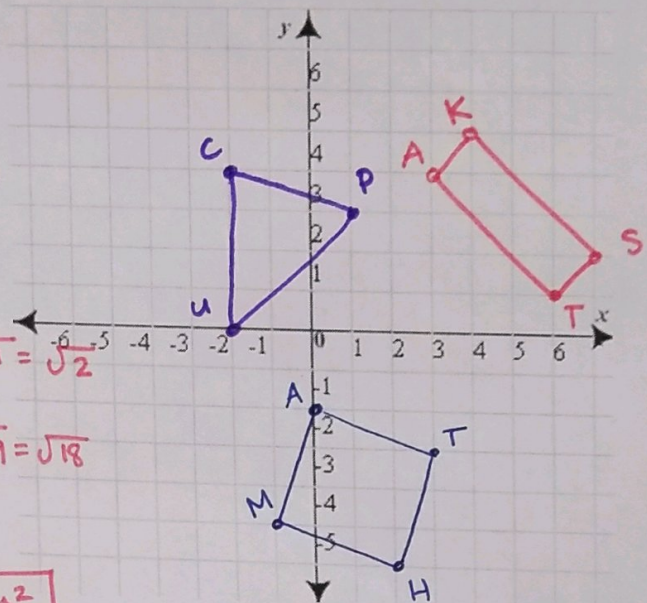
$(-2 + \frac{2}{5}(1-(-2)), -3 + \frac{2}{5}(7-(-3))) \rightarrow (-2 + \frac{2}{5}(3), -3 + \frac{2}{5}(10))$

$(-\frac{4}{5}, 1)$

10. Find the coordinates of point T that lies $\frac{1}{3}$ of the way on the directed line segment \overline{GA} , where $G(4, 6)$

and $A(5, -1)$. $(4 + \frac{1}{3}(5-4), 6 + \frac{1}{3}(-1-6)) \rightarrow (4 + \frac{1}{3}(1), 6 + \frac{1}{3}(-7))$

$(4\frac{1}{3}, 3\frac{2}{3})$ or $(\frac{13}{3}, \frac{11}{3})$



Directions: Write the equation of the line with the given information.

11. A line parallel to $y=3x+4$ and goes through point $(-1, -2)$.

$$\begin{aligned} m: 3 \\ x_1: -1 \\ y_1: -2 \end{aligned} \quad \begin{aligned} y - (-2) &= 3(x - (-1)) \\ y + 2 &= 3(x + 1) \\ y + 2 &= 3x + 3 \end{aligned} \quad y = 3x + 1$$

12. A line perpendicular to $3y+2x=6$ and goes through the point $(3, 3)$.

$$\begin{aligned} m: \frac{3}{2} \\ x_1: 3 \\ y_1: 3 \end{aligned} \quad \begin{aligned} y - 3 &= \frac{3}{2}(x - 3) \\ y - 3 &= \frac{3}{2}x - \frac{9}{2} \end{aligned} \quad y = \frac{3}{2}x - 1.5$$

13. A line parallel to the line that goes through points $(4, 2)$ and $(0, 8)$ and goes through the point $(1, 1)$.

$$\begin{aligned} \frac{8-2}{0-4} &= \frac{6}{-4} = -\frac{3}{2} \\ m: -\frac{3}{2} \\ x_1: 1 \\ y_1: 1 \end{aligned} \quad \begin{aligned} y - 1 &= -\frac{3}{2}(x - 1) \\ y - 1 &= -\frac{3}{2}x + \frac{3}{2} \end{aligned} \quad y = -\frac{3}{2}x + 2.5$$

14. A line perpendicular to the line that goes through points $(3, 0)$ and $(-1, -1)$ and goes through point $(4, 1)$.

$$\begin{aligned} \frac{-1-0}{-1-3} &= \frac{-1}{-4} = \frac{1}{4} \\ m: -4 \\ x_1: 4 \\ y_1: 1 \end{aligned} \quad \begin{aligned} y - 1 &= -4(x - 4) \\ y - 1 &= -4x + 16 \end{aligned} \quad y = -4x + 17$$

15. A line perpendicular to the line that passes through $(1, 2)$ and $(1, -4)$ and goes through the point $(4, 3)$.

$$\begin{aligned} \frac{-4-2}{1-1} &= \frac{-6}{0} = \text{vertical} \perp \rightarrow m: \text{horizontal (0 slope)} \\ x_1: 4 \\ y_1: 3 \end{aligned} \quad \begin{aligned} y - 3 &= 0(x - 4) \\ y - 3 &= 0 \end{aligned} \quad y = 3$$

16. A line parallel to the line $4y+3=2x$ and goes through the point $(-2, -5)$.

$$\begin{aligned} m: \frac{1}{2} \\ x_1: -2 \\ y_1: -5 \end{aligned} \quad \begin{aligned} y - (-5) &= \frac{1}{2}(x - (-2)) \\ y + 5 &= \frac{1}{2}(x + 2) \\ y + 5 &= \frac{1}{2}x + 1 \\ y &= \frac{1}{2}x - 4 \end{aligned}$$