

Solve for all of the zeroes for the following polynomials. You must show the process for finding the zeroes.

26. $x^4 + 3x^3 - x^2 + 27x - 90 = 0$

Factored Form: $(x+5)(x-2)(x^2+9)$

Roots: $-5, 2, \pm 3i$

$$\begin{array}{r|rrrrr} -5 & 1 & 3 & -1 & 27 & -90 \\ & \downarrow & & & & \\ & & -5 & 10 & -45 & 90 \\ \hline 2 & 1 & -2 & 9 & -18 & 0 \\ & \downarrow & & & & \\ & & 2 & 0 & 18 & \\ \hline & 1 & 0 & 9 & 0 & \end{array}$$

$$\begin{aligned} x^2 + 9 &= 0 \\ x^2 &= -9 \\ x &= \pm 3i \end{aligned}$$

27. $g(x) = 2x^5 + 5x^4 - 7x^3 - 11x^2 + 13x - 2$

Factored Form: $(x+2)(x-1)^2(2x^2+5x-1)$

Roots: $-2, 1, \frac{-5 \pm \sqrt{33}}{4}$

$$\begin{array}{r|rrrrrr} -2 & 2 & 5 & -7 & -11 & 13 & -2 \\ & \downarrow & & & & & \\ & & -4 & -2 & 18 & -14 & 2 \\ \hline 1 & 2 & 1 & -9 & 7 & -1 & 0 \\ & \downarrow & & & & & \\ & & 2 & 3 & -6 & 1 & \\ \hline 1 & 2 & 3 & -6 & 1 & 0 \\ & \downarrow & & & & & \\ & & 2 & 5 & -1 & & \\ \hline & 2 & 5 & -1 & 0 & \end{array}$$

$$\begin{aligned} &\frac{-5 \pm \sqrt{(5)^2 - 4(2)(-1)}}{2(2)} \\ &= \frac{-5 \pm \sqrt{33}}{4} \end{aligned}$$

28. What are all of the possible rational roots for $f(x) = 3x^4 - 7x + 48$?

$P: 1, 2, 3, 4, 6, 8, 12, 16, 24, 48$

$Q: 1, 3$

11. $\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 8, \pm 12, \pm 16,$

$\pm 24, \pm 48, \pm 1/3, \pm 2/3, \pm 4/3, \pm 8/3, \pm 16/3$

29. Write a **function** (use proper notation) in factored form, given the following roots: $3i, 5i, 2, -1$.

$$f(x) = (x-3i)(x+3i)(x-5i)(x+5i)(x-2)(x+1)$$

Identify the f

30. $y = -4x^4$

Degree

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Leading

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31. Sketch the g

Zeroes:

Intervals

Intervals

32. Write the equa
rises to the left and

Identify the following for each of the polynomials given.

30. $y = -4x^4 - 2x^2 + 7$

Degree of polynomial: 4

Name by the degree of the polynomial: quartic

of terms: 3

Name by the number of terms: trinomial

Leading coefficient: -4

Maximum number of zeroes: 4

Symmetry of the polynomial: even

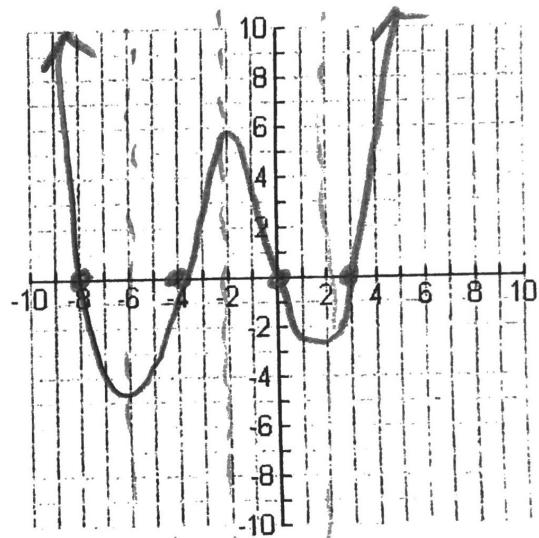
End behavior: $as x \rightarrow -\infty, f(x) \rightarrow -\infty$
 $as x \rightarrow \infty, f(x) \rightarrow -\infty$

31. Sketch the graph of the polynomial function with the following characteristics:

Zeroes: 3, 0, -4, -8

Intervals of increase: $(-6, -2), (1, \infty)$

Intervals of decrease: $(-\infty, -6), (-2, 1)$



32. Write the equation of the function that is a quintic binomial with odd symmetry and whose end behavior rises to the left and falls to the right.

$$y = -x^5 + x^3$$

$\neq 16,$
 $\pm 8/3, \pm 16/3$